

COMPARING THE MEANS OF THREE OR MORE SAMPLES or GROUPS (often called *treatments* in experiments)

THE ANALYSIS OF VARIANCE (ANOVA):

One of the most important and used tools in statistics

















THE ANALYSIS OF VARIANCE (ANOVA) for comparing multiple sample means (groups or treatments)

 \textbf{H}_0 : The samples come from statistical populations with the same mean, i.e., $\mu_{control}=\mu_{knee}=\mu_{eyes}.$

Which is to say:

H₀: Differences in means among groups are due to sampling error from the same population.
H_A: Differences in means among groups are NOT due to

sampling error from the same population.

Remember: Sampling error is due to sampling variation, i.e., samples that come from the same statistical population may differ in their means just due to chance alone.

















HETEROSCEDASTICITY reduces the F-ratio ability to differentiate among differences in means among groups Means among groups are somewhat similar in A than B; A is homoscedastic B heteroscedastic $F_A = \frac{14078.0}{5.71}$ 12275.0 -= 2456.90 $F_B =$ = 56.34 217.9 values Α B response v Fictional r 8 Fictional treatments Fictional treatments

































































The statistical "machinery":

1) Assume that H_0 is true (i.e., samples come from the same population; i.e., population having the same mean and same variance).

2) Sample from the population the appropriate number of groups (samples) respecting the sample size of each group.

3) Repeat step 2 a large (or infinite) number of times and each time calculate the F statistic.

























ANOVA

Assumptions are the same as for the independent two sample t-test:

- Each of the observations is a random sample from its population (whether they are the same or different populations).

- The variable (e.g., shift in circadian rhythm) is normally distributed in each (treatment) population. More on that in another lecture.

- The variances are equal among all populations from which the treatments were sampled (otherwise the F values change in ways that may not measure difference among means). More on that in another lecture.

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"The knees who say night"

 $\begin{array}{l} \textbf{H}_0: \mu_{control} = \mu_{knee} = \mu_{eyes} \\ \textbf{H}_A: \mbox{ at least one population mean } (\mu) \mbox{ is different from another population means.} \end{array}$

Conclusion? Significant, but how?

How do we know which group means differ from one another?

Why not simply not contrast all pairs of means using a two-sample mean t-test? Control vs. knee; control vs. eyes; knee vs. eyes?

More later in the course!