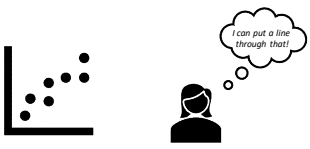


## Simple Linear Regression (Part 1)



Guest Lecture By:  
 Brian Gallagher  
 PhD Candidate  
 Department of Biology

---

---

---

---

---


---

---

---

### Goals for today

- Review basic statistical analyses and the types of variables used
- Introduce linear regression and its applications
- Learn about how regression models are 'fitted' to real data
- Interpreting coefficients from regression models



Where are we going?

---

---

---

---

---

---

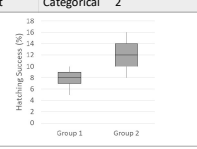
---

---

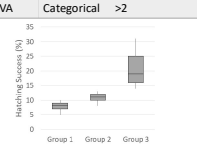
### Statistical analysis

- Science is hard, but statistics help us make inferences based on data
- Many analyses are based on detecting **differences in means**
  - Do means differ in two groups? (t-test)
  - Do means differ across multiple groups? (ANOVA)
- Regression builds directly off these previous analyses
  - Does the mean value of one variable change based on another variable?
  - Uses **continuous variables**

Analysis	Data type	N groups
t-test	Categorical	2



Analysis	Data type	N groups
ANOVA	Categorical	>2



---

---

---

---

---

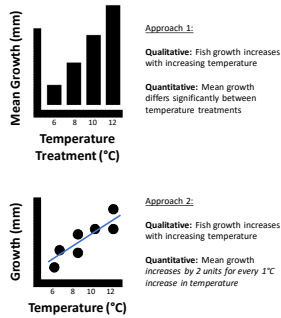
---

---

---

**Categorical vs continuous variables**

- Question: how does fish growth rate respond to increasing temperature?  
- Two possible ways to answer this
- Approach 1: conduct experiments where fish grow in tanks at different temperatures that are precisely controlled  
- Temperature is **categorical** (ANOVA)
- Approach 2: measure growth rates of fish that experience different temperatures in the wild  
- Temperature is **continuous** (regression)
- Very similar qualitatively, but regression provides **different quantitative results**




---

---

---

---

---

---

---

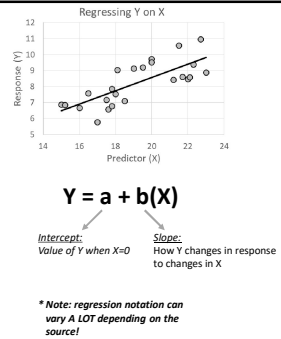
---

---

---

**Regression**

- Regression estimates the relationship between **two continuous variables**  
- Response (Y), or dependent variable  
- Predictor (X), or independent variable
- Y is always **regressed on X**, and relationship is expressed as a linear model  
- Intercept (a)  
- Slope (b)
- Slope and intercept must be **estimated** from the data




---

---

---

---

---

---

---

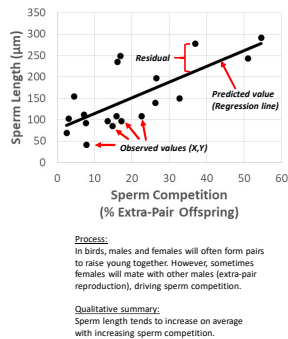
---

---

---

**Fitting regression models**

- Three main components
- Observed values: raw data points with Y and X coordinates
- Predicted values: line predicting the **average value** of Y at each value of X
- Residuals: **differences** between observed and predicted values (on Y-axis)  
- Also called "deviations"
- Ideally, observed and predicted values should be **similar**



Data from: Birkhead and Montgomerie (2020)

---

---

---

---

---

---

---

---

---

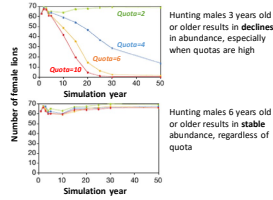
---

**Example: lion conservation**

- Trophy hunting can provide revenue that helps fund conservation initiatives
  - Sustainability is crucial
- Researchers found that hunting **male lions 6 years old or older** had negligible impacts on long-term abundance
  - Driven by social structure and infanticide
- Question: is there an easy way to estimate the age of individual lions?
  - Can help ensure sustainable hunting

**Sustainable trophy hunting of African lions**

Karyl Whitman, Anthony M. Starfield, Henley S. Qualling & Craig Packer  
 Department of Ecology, Evolution and Behavior, University of Minnesota,  
 1987 Upper Buford Circle, Saint Paul, Minnesota 55108, USA



Whitman et al. (2005)

---

---

---

---

---

---

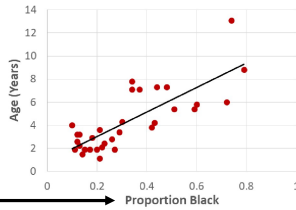
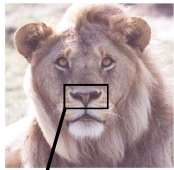
---

---

---

---

**Example: lion conservation**



**Best-fit line:**  
 $Y = 0.88 + 10.65(X)$

**Intercept:**  
 Age=0.88 years when proportion black=0

**Slope:**  
 Age increases by 10.65 years per 1 unit increase in proportion black

Data from: Whitman et al. (2005)

---

---

---

---

---

---

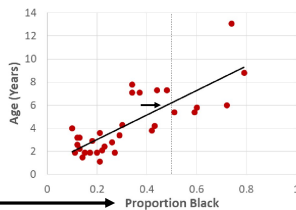
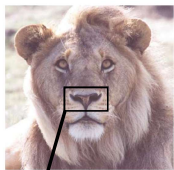
---

---

---

---

**Example: lion conservation**



**Best-fit line:**  
 $Y = 0.88 + 10.65(X)$

Based on this regression line, it is likely that an individual is 6 or older if his nose is **more than 50% black!**

**Lion nose photos can help manage hunting!**

Data from: Whitman et al. (2005)

---

---

---

---

---

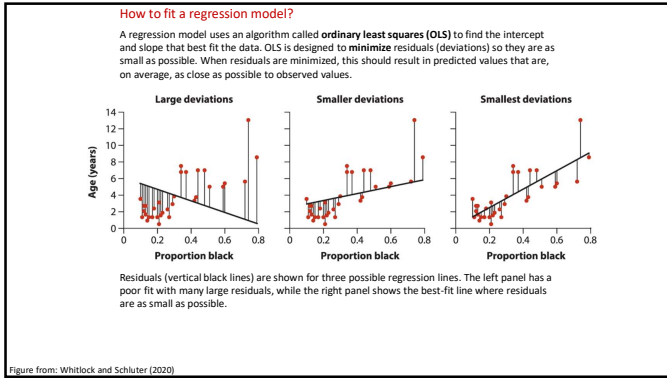
---

---

---

---

---




---

---

---

---

---

---

---

---

---

---

**Note of caution**

- Regression can be useful, but it has limitations!
- Implies a **causal relationship**
  - Need to be thoughtful when choosing X and Y variables
- Avoid extrapolating** far beyond the range of X values that you have
  - If growth is regressed on temperature, which ranges from 5-15°C, do **NOT** use regression to estimate growth at 25°C

**MY HOBBY: EXTRAPOLATING**

Images: Spurious correlations by Tyler Vigen, xkcd comics

---

---

---

---

---

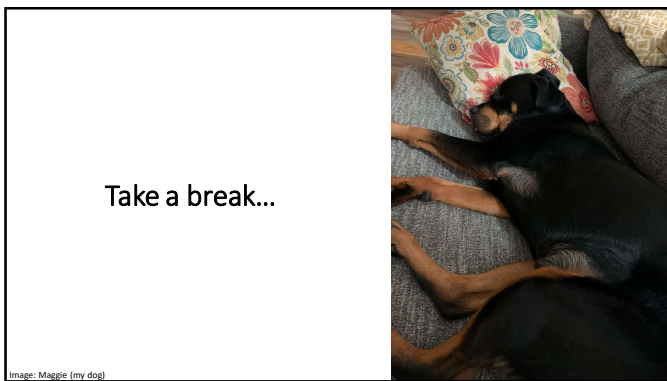
---

---

---

---

---




---

---

---

---

---

---

---

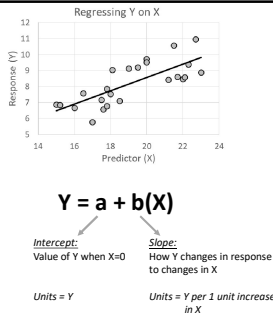
---

---

---

### Regression coefficients

- The intercept and slope are **coefficients** estimated in regression models
- Differences in intercepts and slopes can support inferences
  - Slopes inform the **magnitude and direction** of effects
  - Intercepts can (sometimes) provide a **useful baseline**
- Also important to think about **units**
  - Intercept = Y unit
  - Slope = Y unit/X unit




---

---

---

---

---

---

---

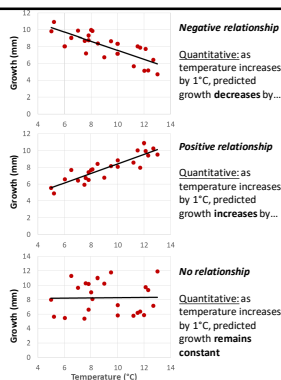
---

---

---

### Slope direction

- Three types of possible relationships
  - Units = mm/°C
- Negative (-)
  - Slope < 0
- Positive (+)
  - Slope > 0
- None
  - Slope = 0




---

---

---

---

---

---

---

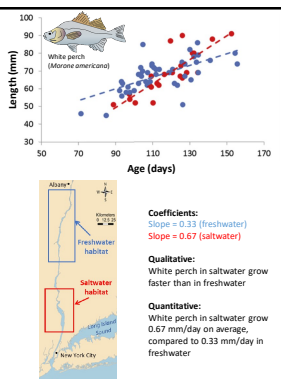
---

---

---

### Slope steepness

- Comparing regression slopes can reveal different **strengths of relationships**
- Example:** white perch in the Hudson River
  - Regressed length on age for individuals caught in freshwater (blue) or saltwater (red) habitats
  - Different slopes**
  - Units = mm/day (growth rate)
- Inference:** average growth rates are **faster** in saltwater than freshwater
  - Slopes tell us *how much* faster (2x)




---

---

---

---

---

---

---

---

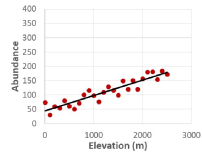
---

---

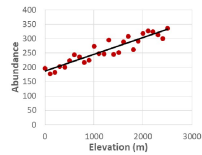
Data: Gallagher et al. (2018). Images: IAN

### Intercept differences

- Comparing regression intercepts can inform **baseline responses**
- **Example:** elevation gradients in abundance
  - Same slope, **different intercepts**
  - Units = abundance (# of individuals)
- **Inference:** species 2 is more tolerant of low elevations than species 1
- Not always ecologically meaningful
  - Depends on X and its units (e.g. a species cannot have negative abundance)
  - Range of X values should include zero



**Species 1:**  
 Slope = 0.05  
 Intercept = 50  
 Quantitative: when elevation is zero (sea level), abundance is predicted to be ~50 individuals



**Species 2:**  
 Slope = 0.05  
 Intercept = 200  
 Quantitative: when elevation is zero (sea level), abundance is predicted to be ~200 individuals

---

---

---

---

---

---

---

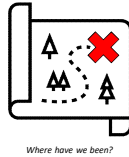
---

---

---

### Overview

- Review basic statistical analyses and the types of variables used
  - Inferences from categorical vs. continuous data
- Introduce linear regression and its applications
  - Estimates the relationship between two continuous variables
- Learn about how regression models are 'fitted' to real data
  - OLS minimizes residuals to find best slope and intercept
- Interpreting coefficients from regression models
  - Intercepts and slopes can support inferences about ecological processes




---

---

---

---

---

---

---

---

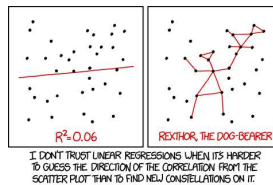
---

---

Thanks!  
 Any questions?

Feel free to e-mail me:

brian.kenneth.gallagher@gmail.com



I DON'T TRUST LINEAR REGRESSIONS WHEN IT'S HARDER TO GUESS THE DIRECTION OF THE CORRELATION FROM THE SCATTER PLOT THAN TO FIND NEW CONSTELLATIONS ON IT

---

---

---

---

---

---

---

---

---

---

Image: xkcd comics