











































The regression line through a scatter of points is described by the following equation:

$$Y = a + bX$$

Y & X are often called by different names across different fields; in biology we often refer to them as:

 $\mathbf{Y}$  is referred as response variable (or also dependent variable).

*X* is referred as explanatory variable (or also independent variable).

## 13

































23

Testing whether the regression slope differs from zero: [1] using a t-test

**H**<sub>0</sub>: the statistical population slope  $\beta = 0$  (i.e., Y can't be predicted by X).

**H**<sub>A</sub>: the population slope  $\beta \neq 0$  (i.e., Y can be predicted by X).

The regression slope b divided by its standard error can be used to test the null hypothesis that  $\beta = 0$ . This is similar to the one-sample t-test:

$$t = \frac{b - \beta_{H_0}}{SE_b} = \frac{b - 0}{SE_b}$$















We can measure the fraction of variation in Y (age) that is "explained" by X in the estimated linear regression model using a quantity called "coefficient of determination" or the "famous" R<sup>2</sup>:  $R^{2} = \frac{SS_{regression}}{SS_{total}}$ The maximum amount of variation in age that could be explained by any linear regression model is the total sum-of-squares of Y (age):  $SS_{total} = \sum_{i=1}^{n=32} (Y_{i} - Y_{i})^{2} = 222.09$ 

28



29



















35

## Using regressions to make predictions (regression of Y on X does not always imply dependency) SPURIOUS CORRELATION

"Predictive capacity without explanatory capacity is worthless. Mere clairvoyance, irrespective of its sharpness, does not itself have scientific standing. Only predictive capacity that arises out of having coherent and communicable explanations has scientific standing. The power to predict is subsidiary to the power to explain. Explanation without prediction is sufficient, but prediction without explanation is of no consequence from a scientific standpoint."

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## Using regressions to make predictions

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## As George E. P. Box said: "All models are wrong, but some are useful"



38















Let's say a lion with 50% of their noses covered by black spots is being considered for

The prediction is 6.2 years of Age! How much can we trust

Unfortunately, the confidence is not very good! Under normality assumptions, we are 95% confident (a good chance) that an individual with 50% of blad constr. avaid with 50% of black spots could be between 1.7 and 9.7 years.

































































