





2

The Pearson's correlation coefficient measures the strength and direction of the association between two continuous variables - *it measures the tendency of two variables to co-vary.*

Unlike linear regression -1) correlation fits no line to the data; and 2) there are no expectation in terms of which variable is the response and which variable is the predictor.

$$r = \frac{\sum_{i=1}^{n} (X_i - X)(Y_i - Y)}{\sqrt{\sum_{i=1}^{n} (X_i - X)^2} \sqrt{\sum_{i=1}^{n} (Y_i - Y)^2}} \quad \begin{array}{l} \text{Y = log (brain mass)} \\ \text{X = log (body mass)} \end{array}$$

The numerator is called sum of products, and it measures how the deviations in X and Y (from their means) vary together.

The denominator assures that r always varies between -1 and 1.

The formula for the (Pearson's) correlation coefficient (r) has three parts, two of which should look familiar, and one should be new (to you).



























Parametric tests and their assumptions – one sample & two sample t-tests, ANOVA, regression and correlation
General Assumptions of parametric tests (the way the assumption is tested may change between approaches):
1) Observations are random.
2) Data are homoscedastic
3) Samples are normally distributed

Test	Advantages	Disadvantages	
Chi-Square test	 appropriate for any level of measurment ties may be problematic 	 grouping of observations required (frequencies per group must be > 5) unsuitable for small samples statistic based on squares 	
Kolmogorov-	suitable for small samples	no categorial data	
Smirnov test	 ties are no problem omnibus test 	 low power if prerequisites are not me 	
Lilliefors test	higher power than KS test	no categorial data	
Anderson-Darling	high power when testing for normal	no categorial data	
test	 more precise than KS test (especially in the outer parts of the distribution) 	 statistic based on squares 	
Shapiro-Wilk test	highest power among all tests for	test for normality only	
	nomaity	 complicated procedure 	
Cramér-von-Mises	higher power than KS test	statistic based on squares no categorial data	







Assessing the normality assumption: The Quantile-Quantile normal plot (Q-Q normal plot)

The Q-Q plot is a graphical technique for determining if multiple samples come from populations with a common distribution (here, if they all come from normally distributed populations).

It plots the quantiles (also known as percentiles) of the data against the quantiles of a normally distributed population.

Percentiles are values in the data below which a certain proportion of your data fall. The median is the 50% quantile (or percentile) because 50% of the data follows below that value and 50% above that value.

Go back to our lecture on interquartile range: instead of thinking in terms of 25%, 50% and 75% quartiles (which divide the data into quarters), think of much smaller quantiles that divide the data into 20 pieces (every 5%) or even 100 pieces (every 1%).









The Qu	antile-Qua	intile norm	all plot (Q-0	Q normal plot)
t's divide the	e data into ev	ery 5 percen	tile points: no	ote how the differen
e middle poi % & 10% · 90	nts (40%, 45° Դ% & 05%)	%, 50%) are	more similar	than points in the t
/0 & 10 /0, 50	J /0 & 3J /0j.			
_	_	_	_	
•••				
quant.data			l,probs = se	q(0.05,0.99,0.05)
<pre>quant.data > quant.data 5%</pre>			l,probs = sei 20%	q(0.05,0.99,0.05) 25%
<pre>quant.data - > quant.data 5% -1.76124237</pre>			20% -0.76795073	q(0.05,0.99,0.05) 25% -0.67175383
<pre>quant.data + > quant.data 5% -1.76124237 30%</pre>			20% -0.76795073 45%	q(0.05,0.99,0.05) 25% -0.67175383 50%
<pre>quant.data - quant.data 5% -1.76124237 30% -0.45899733</pre>			20% 20% -0.76795073 45% -0.05423166	q(0.05,0.99,0.05) 25% -0.67175383 50% 0.02656021
<pre>quant.data + quant.data +</pre>	<- quantite() a -1.34993425 35% -0.27668011 60%		20% 20% -0.76795073 45% -0.05423166 70%	q(0.05,0.99,0.05) 25% -0.67175383 50% 0.02656021 75%
<pre>quant.data + quant.data +</pre>	<pre><- quantitie() a</pre>		20% -0.76795073 45% -0.05423166 70% 0.42498326	q(0.05,0.99,0.05) -0.67175383 50% 0.02656021 75% 0.67732982
<pre>quant.data > quant.data 5% -1.76124237 30% -0.45899733 55% 0.16567709 80%</pre>	<pre><- quantitie() a</pre>	15% -1.13526610 -0.13026546 65% 0.33267221 90%	20% -0.76795073 45% -0.05423166 70% 0.42498326 95%	q(0.05,0.99,0.05) 25% -0.67175383 50% 0.02656021 75% 0.67732982
<pre>quant.data > quant.data 5% -1.76124237 30% -0.45899733 55% 0.16567709 80% 0.82123220</pre>	<pre><- quantities a</pre>		20% -0.76795073 45% -0.05423166 70% 0.42498326 95% 1.63890087	25% 25% -0.67175383 0.02656021 75% 0.67732982





































Relaxing the normality assumption: non-parametric hypotheses tests

29

Parametric *versus* non-parametric hypotheses tests

A **parametric** statistical **test** is one that makes assumptions about the parameters (defining properties) of the population distribution(s) from which one's data are drawn, while a **nonparametric test** is one that makes "no such assumptions".

Source - http://vassarstats.net/textbook/parametric.html

Tests we covered so far assumed normality and equality of variance (means and regression).







32

Parametric tests assuming normality (e.g., t-test & ANOVA) are affected by non-normality; depending on the type of non-normality (shape), parametric tests can have either inflated type I errors (i.e., type I error rates greater than alpha) or lower power (i.e., increased type II errors).

Br J Mam Sait Peychol. 2013 May:68(2):224-44. doi: 10.1111/j.2044-8317.2012.02047.x. Epub 2012 May 24. The impact of sample non-normality on ANOVA and alternative methods. Lantz B¹.

Author information

Abstract

In this journal, Zimmerman (2004, 2011) has discussed preliminary tests that researchers often use to choose an appropriate method for comparing locations when the assumption of normality is doubtful. The conceptual problem with this approach is that such a two-stage process makes both the power and the significance of the entre procedure uncertain, as type I and by the I errors at possible at both stages. A type I error at the first stage, for example, will obviously increase the probability of a type II error at the second stage. Based on the dea of Schmider et al. (2010), which propreses that simulated sets of sample data be transide with respect to the performance of the ANOVA, Brown-Forsythe test, which test, and Kouskal-Wallis test when used with different distributions, sample size, and effect sizes. The overall conclusion is that the Kruskal-Wallis test considerably less sensitive to the degree of sample normality when populations are distingly non-normal and should methore be the primary tool used to compare locations when it is known that populations are not at test.

Non-parametric tests are those that can handle non-normal data (but the assumption of homoscedasticity is also important though not usually verified)

These are the main non-parametric tests used in Biology for comparing samples:

1) For comparing two samples (analogue of the parametric two sample t-test) – *The Mann–Whitney U-test* (also known as the Mann–Whitney–Wilcoxon test, the Wilcoxon rank-sum test, or the Wilcoxon two-sample test).

2) For comparing multiple samples (analogue of the parametric ANOVA) – *The Kruskal-Wallis test.*

The P-value for the The Mann-Whitney U-test and the The Kruskal-Wallis test is mathematically the same and we will cover only the latter.

Note: we covered t-tests separate from ANOVA for three reasons: one sample t-tests, understand the nature of post-hoc testing (e.g., pairwise comparison of means after ANOVA) and because there is a t-test dealing with samples having different variances (though there is a very complex ANOVA version as well).

34

genetic polymorphism) in two populations of the American oyster. Crossstrue sityainia, Medbonald et al. (1996) collected data on Esy for eix anonymous DNA polymorphisms (variat in random bits of DNA of no known function) and compared the Esy values of the six DNA ophymorphisms to Exp values on 3D proteins from Binnetwe (1983). The biological question was whether potein polymorphisms Would have generally lower or higher Esy values that anonymous DNA of propulsystems Would have generally lower or higher Esy values that anonymous DNA of propulsystems Would and est (1998) the biological question was defined for two populations is highly skewed, so they analyzed the detuction of estimates test. stion was test. When worki the rank in the Non-parametric tests (including the Kruskal-Wallis test) Winc. the rank in the ov the second-small two F_{st} values of ata set for each measurement value. The smallest value sets a rank of a rank of a rank of a rank of 2, etc. The observationally a value of 2.5 and a land the transformations we test for second and third, so they get a rank of 2.5. Example: FST is a measure of the amount of
 gene
 class
 F_{ST}

 CVJ5
 DNA
 -0.006

 CVB1
 DNA
 -0.005
 geographic variation in a genetic polymorphism. Here, McDonald et al. (1996) compared two
 CV15
 DNA
 -0.005

 CV81
 DNA
 -0.005

 GP2d
 protein
 -0.005

 GP2d
 protein
 -0.005

 GP2d
 protein
 -0.005

 Est-3
 protein
 -0.005

 Est-3
 protein
 0.004

 Lap-2
 protein
 0.016

 Adk-1
 protein
 0.014

 Agr-3
 protein
 0.014

 Agr-3
 protein
 0.044

 Lap-1
 protein
 0.044

 Mpi-2
 protein
 0.048

 CV16
 DNA
 0.085

 CV16
 DNA
 0.095
 populations of the American oyster regarding the Fsr based on six anonymous DNA polymorphisms (variation in random bits of DNA of no known function) and compared the FsT values of the six DNA polymorphisms to FsT values on 13 proteins. Question: Do protein differ in FST values in contrast to anonymous DNA polymorphisms? Zero Fst = no genetic variation (panmictic) **negative F**_{ST} = more genetic variation within populations than between the two populations being compared. positive Fst = more variation between populations than Est-1 protein 0.163 within the two populations being compared. sum of the ranks for each group, then the test statistic, H. H is given by a mula that basically represents the variance of the ranks among groups, or the number of test. His approximately divising and the statistic, meaning greating a particular value of H by chance, if the null hypothesis is true great from McDonald et al. (1996) and great and the statistic of the statistic of the number of the statistic with an adjust that the proba the P value co groups minus 1.February 1.Februa the rank in the overa the second-smallest two F_{st} values of -0.0 rets a rank of 2 or 1 of aber atime set as recently in the data of thank transformations class F_{ST} Rank Rank gene DNA -0.006 1 DNA -0.005 2.5 CVI5 CVB1 (2+3)/2=2.5 2.5 6Pgd protein -0.005
 Pgi
 protein
 -0.002

 CVL3
 DNA
 0.003

 Est-3
 protein
 0.004
 4 5 6 Lap-2 protein 0.006
 Pgm-1
 protein
 0.015

 Aat-2
 protein
 0.016

 Adk-1
 protein
 0.016
 9.5 (9+10)/2=9.5 9.5 Sdhprotein0.024Acp-3protein0.041Pgm-2protein0.044 11 Acp-3 12 13
 Image: 14 15 16
 Ap-1
 protein
 0.066

 CVJ6
 DNA
 0.095

 CVB2m
 DNA
 0.116
 17 18 19 Est-1 protein 0.163 20 http://www.biostathandbook.com/kruskalwallis.html Data from McDonald et al. (1996) f the ranks for each group, then the test statistic, H. H is given by a You calculate the

You calculate the sum of rather formidable fo with an adjustment that the probability .36 the P value correspo groups minus 1. For protein is 10.68, H=(hypothesis that the 1 reliefted

rejected.

For the reasons given above, I think it would actually be better to analyze the oyster data with one-way anova. It gives a P value of 0.75, which fortunately would not change the conclusions of McDonald et al.













Kruskal-Wallis test

What is the probability that a randomly sampled observation from population **P** is greater (or smaller) in rank than a randomly sampled observation from **Q**? If the probability is small, then the samples come from different populations; **in other words, a sample dominates another sample.**

H₀: no sample dominates another sample.

 H_A : at least one sample dominates one other sample.

Varga and Delanay (1998)

40





41 ic polymorphism) in two popu mald et al. (1996) collected data





genetic polymorphism) in two populations of the American systex, Cossotter arriginica. McDonald et al. (1996) collected data on effect for asi anonymous ORNA polymorphisms (variation in mandem bits of DNA of no known functions) and compared the Vig- values of the six DNA effect of the six DNA which erynoites polymorphisms would also generally lower or higher Ery values that anonymous DNA polymorphisms. McDonald et al. (1996) know that the therewical distribution of Ery for two populations is highly showed, when yand polymorphisms and all also when also also data of the American Six of the Six of th





genetic polymorphism) in two populations of the American oyster. Consostron ringinica McDanial et al. (1996) callected data on Fg for six anonymous DNA polymorphisms (variatili in mandm bits of DNA of no known functional) and compared the first yealses of the six DNA polymorphisms in Fg values on 51 proteins from Barabeet (1983). The biological question was whether protein polymorphisms. McDanald et al. (1994) know that the three that anonymous DNA polymorphisms. McDanald et al. (1994) know that the three McLanal-Wallis







Kruskal-Wallis test – statistic H

Assumptions:

- Independent samples
- Homoscedasticity of ranks (not commonly tested and the Levene's test can be used to test for this assumption) – test the distribution of ranks instead of original values.