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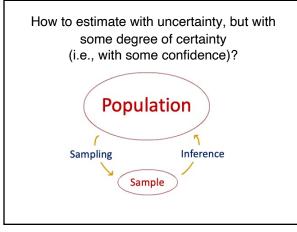
Statistics - like life itself - is all about making big conclusions from (small) samples.

One primary goal of statistics is to estimate (infer) an unknown quantity (parameter) of a population based on sample data.

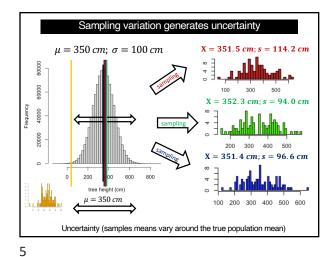
Estimation involves inferring a population parameter (e.g., mean, standard deviation, median) from a sample.

We use estimates to make decisions. Statistics is fundamentally the science of making decisions with incomplete knowledge, often using samples from populations of unknown sizes.

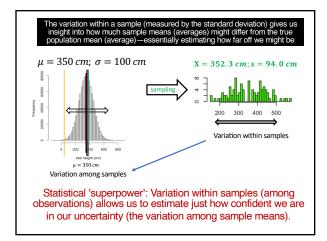
However, sample-based statistics (e.g., mean, median, standard deviation) vary from one sample to another. This variation introduces uncertainty, known as sampling variation.













Population parameters versus sample estimates

A parameter describes a quantity in a statistical population, while an estimate (or statistic) is a similar quantity derived from a sample.

For example, the mean of a population is a parameter, whereas the mean of a sample is an estimate (or statistic) of the population mean.

Similarly, the standard deviation of a population is a parameter, and the standard deviation of a sample is an estimate (or statistic) of the population's standard deviation.

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Estimating with uncertainty (i.e., error around the true parameter)

An estimate (derived from a sample) is rarely, if ever, exactly the same as the population parameter being estimated-especially in large populations-because sampling is influenced by chance.

For example, two people could sample 100 trees from the same forest and get different mean values. Neither of these sample means will be exactly equal to the population mean.

The critical question in statistics is: In the face of uncertainty (due to random chance), how much can we trust an estimate and the decisions based on it? In other words, how accurate is the estimate (i.e., how close is the sample value to the true population value)?

The goal is to deal with uncertainty with a degree of certainty!

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How to estimate with uncertainty, but with some degree of certainty (i.e., with some confidence)?

We need to understand the properties of estimators (such as the mean, variance, and standard deviation).

These **properties** are examined through the sampling distribution of the statistic or estimate of interest (e.g., sample mean, standard deviation).

A sampling distribution represents the probability distribution of an estimate based on random sampling from the population. It shows what we might observe if we were to repeatedly sample from the population.

While sampling distributions resemble frequency distributions, sampling distributions are made of probabilities instead of frequencies.

Statistical symbols

 μ = population mean (we say "mu", Greek alphabet). σ = population standard deviation (we say "sigma"). σ^2 = population variance (we say "sigma squared").

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Important statistical symbols regarding inference

 μ = population mean (we say "mu", Greek alphabet).

 σ = population standard deviation (we say "sigma").

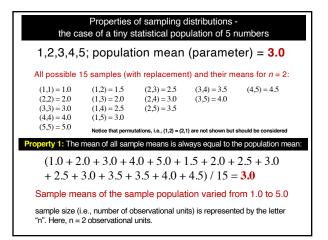
 σ^{2} = population variance (we say "sigma squared").

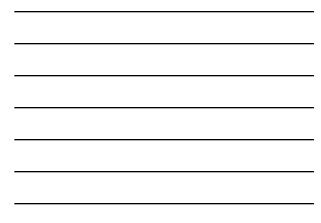
X = sample mean (we say "X bar", Latin or Roman alphabet).

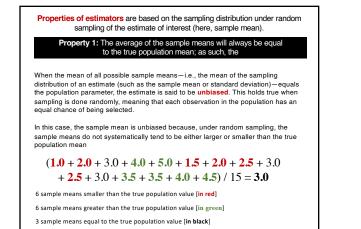
s = sample standard deviation.

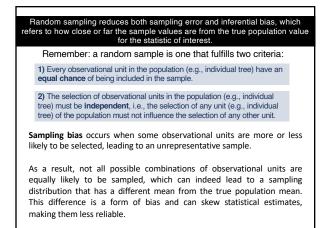
s² = sample variance.

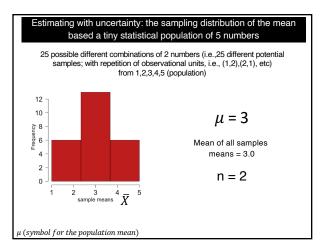
While μ always represent the mean of the population for any variable you're measuring (e.g., X), the symbol for the sample mean (as discussed before) can vary depending on the variable. For example, it might be written as X for the mean of X, or Y for the sample mean of Y. However, the key is that it always includes a bar on top of the variable, regardless of which variable you're referring to.



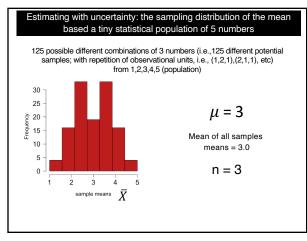




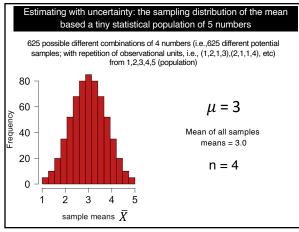




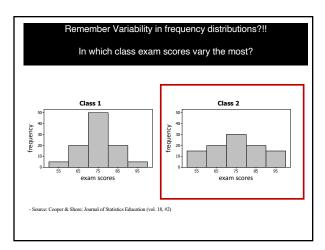




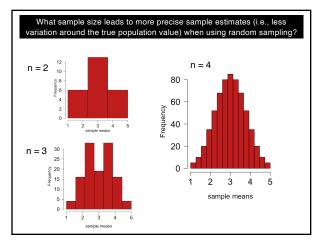


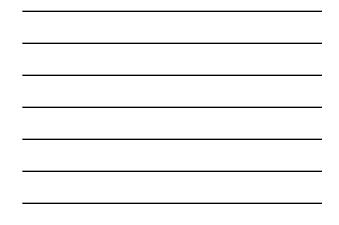


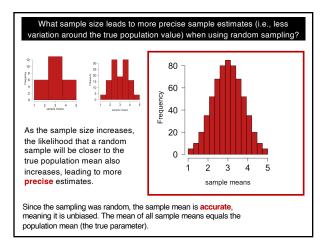


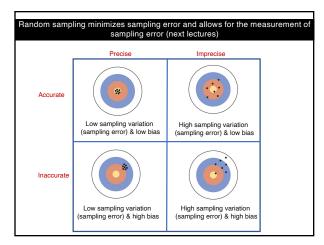




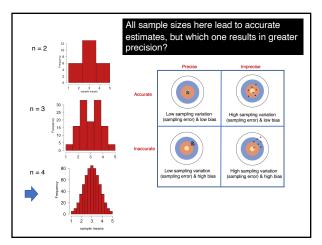




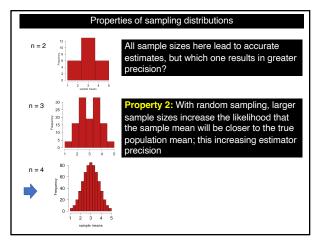




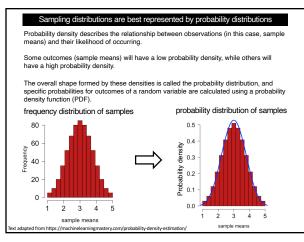




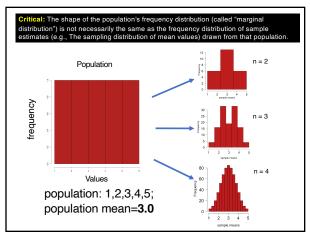




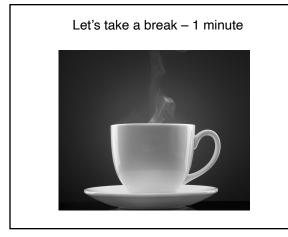


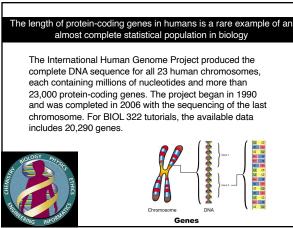




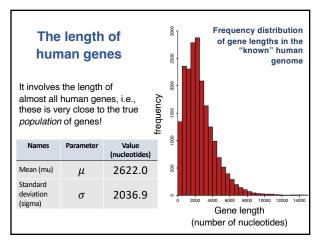














In real situations, we typically don't know the parameter values of the study population, but in this case, we (almost) do! So, we'll take advantage of this gene population to illustrate the processes of sampling, uncertainty, accuracy, precision, and how to estimate with uncertainty—yet with some level of confidence!

