Job trends in statistics and data analysis

With so much hinging on statistics - national and international policy, funding, corporate decision making, government commitment and research - **demand for statisticians and data analysts is expected to grow around 34% between 2014 and 2024**. This vastly outstrips the average across all jobs.

source - https://www.environmentalscience.org/career/environmental-data-analyst







3







	Linear Model	Common name			
	$Y = \mu + X$	Simple linear regression			
	$Y = \mu + A_1$	One-factorial (one-way) ANOVA			
	$Y = \mu + A_1 + A_2 + A_1 \times A_2$	Two-factorial (two-way) ANOVA			
	$\mathbf{Y} = \boldsymbol{\mu} + \mathbf{A}_1 + \mathbf{X} \left(+ \mathbf{A}_1 \times \mathbf{X} \right)$	Analysis of Covariance (ANCOVA)			
	$Y = \mu + X_1 + X_2 + X_3$	Multiple regression			
>	$Y = \mu + A_1 + g + A_1 \times g$	Mixed model ANOVA			
	$Y_1 + Y_2 = \mu + A_1 + A_2 + A_1 \times A_2$	Multivariate ANOVA (MANOVA)			
	Y (response) is a continuous variable X (predictor) is a continuous variable A represents categorical predictors (factors) g represents groups of data (more on this later) $(+A_1 \times X)$ - step 1 on an ANCOVA, but not in the final analysis Multiple factors $A_1 + A_2$ + etc (and their interactions)				

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Fixed versus random effects may depend on the question and not always the data

STUDY: Suppose five cuts of meat are taken from each of three pigs, all from the same breed, and the fat content is measured in each cut.

FIXED EFFECT QUESTION – Do the different cuts differ in their fat content? One-way (fixed) ANOVA with five treatment levels (cuts) and three replicates per cut (pigs).

	•	cut.weights 🗘	cut.factor ‡	pig 🗘
	1	1.1	1	1
	2			
plg1 <- c(1.1,2.1,3.1,4.1,5.1) pig2 <- c(1.2,2.2,3.2,4.2,5.1)	3			
pig3 <- c(0.9,2.3,3.1,4.2,5.2)	4			
	5			
<pre>cut.weights <- c(pig1,pig2,pig3) cut factor <- as factor(rep(1:5,3))</pre>	6			
pig <- as.factor(c(rep(1,5),rep(2,5),rep(3,5)))	7			
<pre>View(cbind(cut.weights,cut.factor,pig))</pre>	8			
anova(lm(cut.weights~cut.factor))	9			
	10			
	11			
	12			
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	•	cut.weights 🗘	cut.factor 🗘	pig ‡
$pig1 \le c(1.1,2.1,3.1,4.1,5.1)$ $pig2 \le c(1.2,2.2,3.2,4.2,5.1)$				
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anova(lm(cut.weights~cut.factor))				
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Response: cut.weights Df Sum Sq Mean Sq F value Pr(>F)	15	5.2	5	3
cut.factor 4 30.6293 7.6573 883.54 1.07e-12 *** Residuals 10 0.0867 0.0087				
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Fixed versus random effects may depend on the question and not always the data

STUDY: Suppose five cuts of meat are taken from each of three pigs, all from the same breed, and the fat content is measured in each cut.

FIXED EFFECT QUESTION – Do the different cuts differ in their fat content? One-way (fixed) ANOVA with five treatment levels (cuts) and three replicates per cut (pigs).

RANDOM EFFECT QUESTION - Is there more variation in fat content among or within pigs (i.e., animal-to-animal and withinanimal variation)? A fat pig could have their cuts fatter (i.e., hierarchical variation).

In this case, the three pigs selected are not of interest. This would be a one-way random effects ANOVA.

























27

Hierarchical (clustered) sampling

As a result, in a clustered sample selecting, an additional observation from the same cluster adds less new information than would a completely independent selection. As such, the sample is not as variable a random sample would be, so that the effective sample size is reduced. The loss of effective sample size by using clustered sampling, instead of simple random sampling, is called **design effect**.









Hierarchical (clustered) sampling

The **design effect** is a correction factor that is used to adjust the sample size based on clustered sampling. This accounts for the loss of information inherent in the clustered design and is used when estimating random effects.

Once the design effect is calculated, the sample size calculated for a standard design can be adjusted accordingly (i.e., degrees of freedom are corrected). As such, the statistical power may change according to the design effect.













Hierarchical (clustered) sampling – intraclass correlation & design effect (one extreme example)

Consider a study that wants to estimate fish size between two regions in Quebec (Laurentians and Eastern Townships).

- Draw a random sample of 50 lakes in each region.
- Randomly sample 10 individuals in each lake (*n* = 10).

One fixed factor = region (these two regions cannot change). One random factor = lakes (because they are more likely to be similar within regions and they are not crossed between regions, i.e., lakes differ).







- Draw a random sample of 50 lakes in each region.
- Randomly sample 10 individuals in each lake (n = 10).
- Assume for the sake of discussion that all individuals within each lake had the exact same size but size differed between each of the lakes, then intraclass correlation = 1 and a design effect = 1 + 1(50 - 1) = 50.
- In this case, we have started our sample with 500 individuals across lakes, but the "design" can only "use" 50 values ("observations") in the analysis because all individuals were too similar within lakes! So, to increase the degrees of freedom, we would need to sample now 500 lakes per region instead! So, this design effect reduced the statistical power of the ANOVA.







Mixed models mix random and fixed effects and allows estimating conducting statistical testing (inference) via proper estimation of design effects for hierarchical (clustered) sampling! It also affects parameter estimation (e.g., Simpson's paradox)

41

Why consider a mixed-model? Some factors you may be able to control (fixed) and others you won't (random)

- Models using random effects are important for inference when analyzing data that exhibit non-independence (hierarchical structure).
- (ii) Random effects provide a unifying statistical framework for models that might otherwise seem unrelated, for example, time-series models for populations, spatial models, genetics models, and models for variation among individuals;
- (iii) Models that include random effects are increasingly easy to build and customize for specific problems using publicly available modelling tools and software.

adapted from Thorson and Minto



Mixed models mixes random and fixed effects!

(next lecture)