# Multivariate Analysis: Redundancy Analysis (RDA) BIOL 650 - Alex Engler Guest lecture - 11/04/2023

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### **Outline**

Introduction

1. What is a RDA?

2. Constrained and Unconstrained Variances

3. Plotting and interpreting the RDA

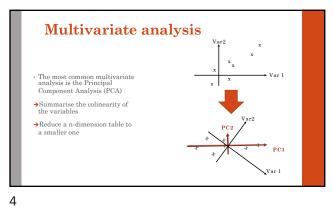
4. Variance partitioning

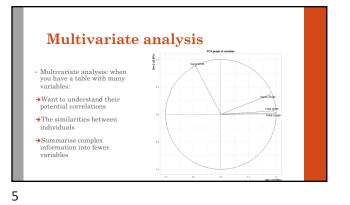
5. Exercice (We will go through a RDA together)

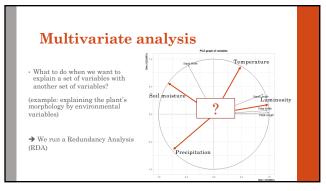
7. Question session

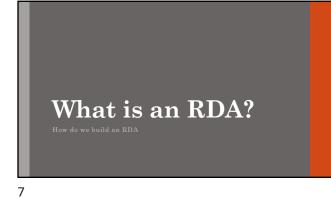
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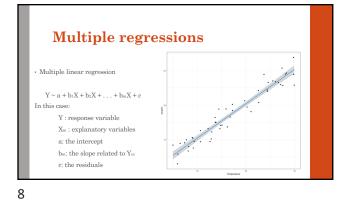


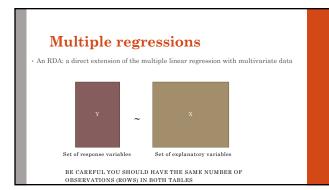




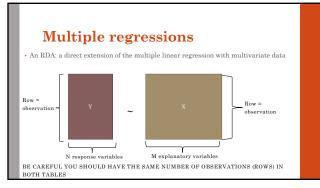




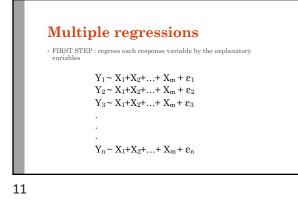


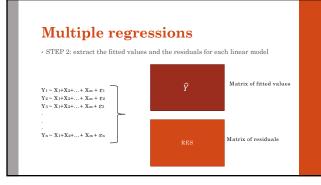




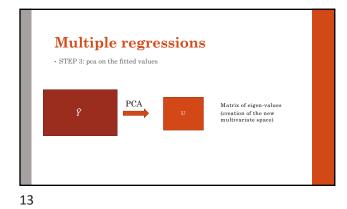


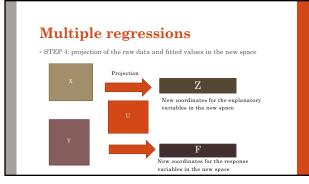


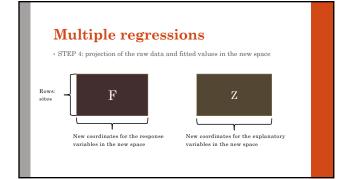




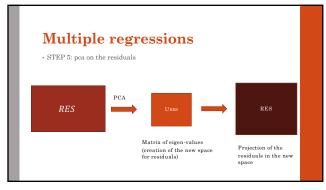












### How do we build an RDA

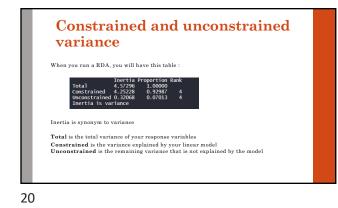
- An RDA is two PCAs in a trenchcoat: • One on the fitted values (summarising the results of multiple linear
- régressions) • One on the residuals (summarising the variability that was not catch by the linear régressions)

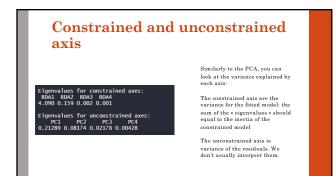


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## The results of the RDA







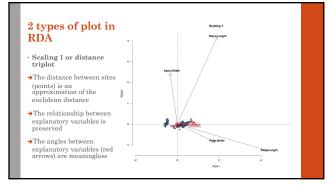
### The performance of the RDA

- Similarly to a regular linear regression, you have a  $\rm R^{2},$  that represents the overall fit of the models (the adjusted  $\rm R^{2}$  take in account the number of explanatory variables)
- $\boldsymbol{\cdot}$  There is F-statistics that compare the model with a null model
- →H₀: the strength of the linear relationship, measured by the canonical R2, is not larger than the value that would be obtained for unrelated Y and X matrices of the same sizes
- $\Rightarrow We \ can test for the whole model or for each axis of the model or for each explanatory variables !$

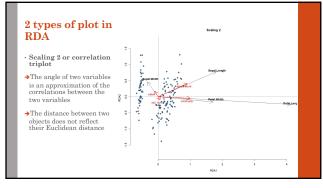
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### Summary

• An RDA is just a linear regression with multiple response variables and multiple explanatory variables

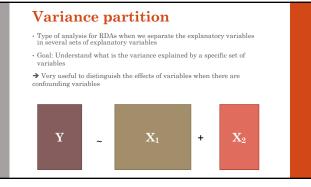
 $\mathbf{Y}\sim\mathbf{X}+\mathbf{R}\mathbf{E}\mathbf{S}$ 

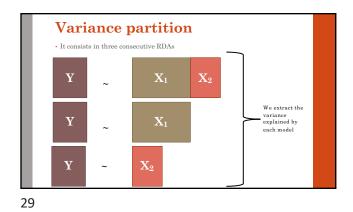
• An RDA is two PCA: one that will capture the variance of the linear models and the other the residuals

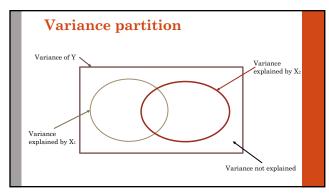
 You can either plot accurately the distance between observations or the relationships between the response variables. In both case, the correlations between response and explanatory variables is conserved

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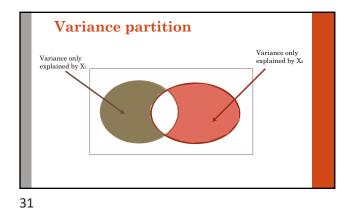
Variance partitioning in RDAs



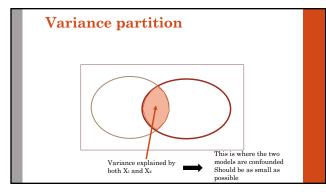










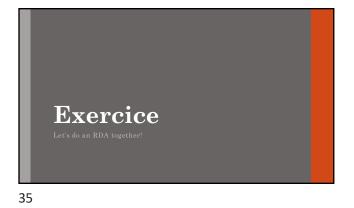


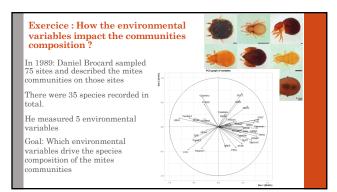
### Summary of the variance partitioning

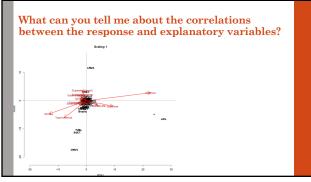
#### It is a method to understand where confounding effects are in our models : How much of the variance could have been explained by different variables ?

- $\stackrel{\bullet}{\rightarrow} \operatorname{Can}$  be very useful when you have geographically structured data
- What to do when you have a lot of shared variance between two variables:
- $\stackrel{\bullet}{\rightarrow}$  You can not separate the effect of one or the other
- $\rightarrow$  You have to redesign your experiment/data collection to be able to separate the effects of the two variables

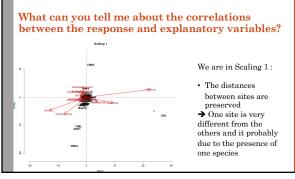


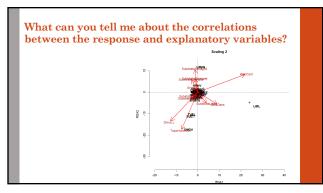




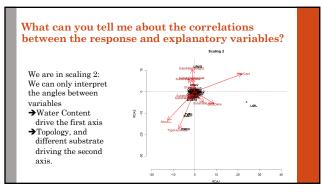




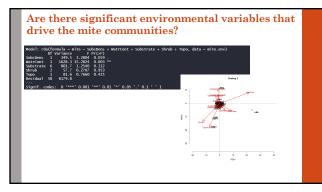




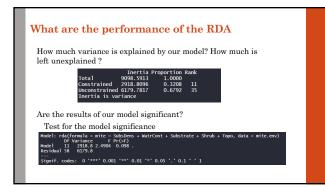


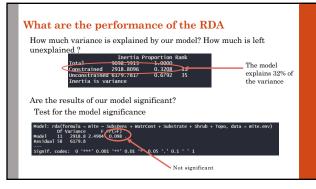












### TIPS TO RUN A RDA

• SCALE YOUR EXPLANATORY AND RESPONSE VARIABLES (avoid to detect effect solely due to difference of units)

 Try to reduce as possible collinearity between explanatory variables as much as possible before running the rda (with a PCA, for instance)

• Make sure you have the good number of observations in both set of variables

· Don't forget to check the percentage of explained variance

You can do a variance partition to desentangle the specific effect of one set of variables

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### Bibliography

Legendre, P., & Legendre, L. (2012). Numerical ecology. Elsevier

Iris dataset: Anderson, Edgar (1935). The irises of the Gaspe Peninsula, Bulletin of the American Iris Society, 59, 2–5 (found in "datasets" package)

Mite dataset: Borcard, D., P. Legendre and P. Drapeau. 1992. Partialling out the spatial component of ecological variation. Ecology 73: 1045-1055. (found in "vegan" package)



Thank you for listening