

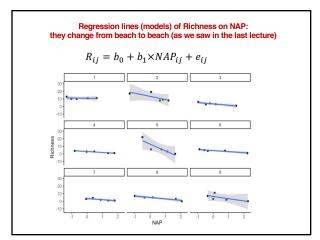
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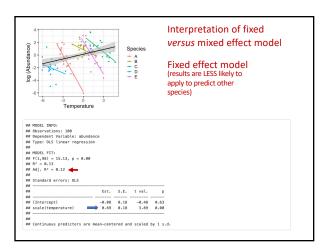
As we will see, once we consider the hierarchical nature of data, different models can be set and made compete to describe the same set of data  $R_{ij} = b_0 + b_1 \times NAP_{ij} + b_2 \times Exposure_j + e_{ij}$ Each site for each beach One value per beach has a NAP value ţ categorical predictor Continuous predictor (ANOVA) Fixed (regression) Mixed effect models ANCOVA You may not be able to see it right now, but there are 10 or more possible linear models (covered in the tutorial) for these data; and one of them will best describe the data (i.e., best at predicting Richness)

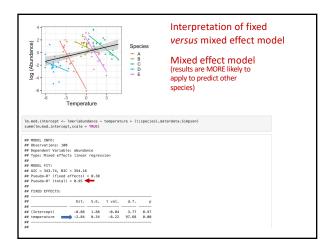
Let's concentrate on NAP for now particularly because it changes from beach to beach whereas Exposure does not (i.e., NAP may have a hierarchical dependence and exposure not)

$$R_{ij} = b_0 + b_1 \times NAP_{ij} + b_2 \times Exposure_j + e_{ij}$$
 Each site for each beach has a NAP value One value per beach

$$R_{ij} = b_0 + b_1 \times NAP_{ij} + e_{ij}$$







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RANDOM INTERCEPT MODEL: assumes a common slope and allow intercept to vary; IS THIS A GOOD MODEL for these data?

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RANDOM INTERCEPT MODEL: assumes a common slope and allow intercept to vary; IS THIS A GOOD MODEL for these data?

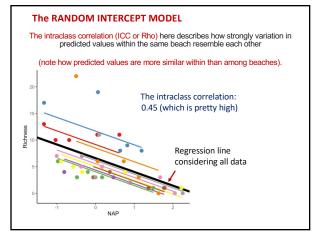
Random effects:
Groups Name Variance Std.Dev.
factor_Beach (Intercept) 7.507 - 2.740
Residual 9.111 - 3.018
Number of obs: 45, groups: factor_Beach, 9

Fixed effects:
Estimate Std. Error df t value Pr(>|t|)
(Intercept) 6.5844 1.0321 9.4303 6.380 0.000104 ***
NAP -2.5757 0.4873 38.2433 -5.285 5.34e-06 ***

The intraclass correlation (ICC or Rho) here describes how strongly variation in predicted values within the same beach resemble each other.

ICC = 7.507 / (7.507 + 9.111) = 0.45 (which is pretty high)
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11

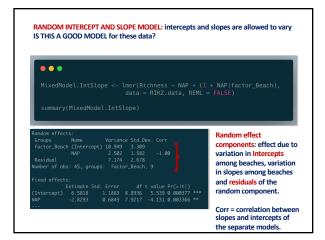


RANDOM INTERCEPT AND SLOPE MODEL: intercepts and slopes are allowed to vary IS THIS A GOOD MODEL for these data?

| MixedModel.IntSlope <- lmer(Richness ~ NAP + (1 + NAP) factor\_Beach), data = RIKZ.data, REML = FALSE)
| summary(MixedModel.IntSlope)

| NAP is the fixed predictor of interest.
| (1 + NAP | factor\_Beach) is the random effect term, where the 1 denotes that we should consider variation in intercepts and also variation in slopes of NAP among beaches, i.e., NAP | factor\_Beach, i.e., we are nesting sites within beaches to form the random effect.

13



14

RANDOM INTERCEPT AND SLOPE MODEL: intercepts and slopes are allowed to vary IS THIS A GOOD MODEL for these data?

MixedModel.IntSlope <- lmer(Richness ~ NAP + (1 + NAP|factor\_Beach), data = RIKZ.data, REML = FALSE)

summary(MixedModel.IntSlope)

Random effects:
Groups Name Variance Std.Dev. Corr
factor\_Beach (Intercept) 10.949 3.309
Residual NAP 2.502 1.582 -1.00
Residual 7.174 2.678
Number of obs: 45, groups: factor\_Beach, 9
Fixed effects:
Extimate Std. Error df t value Pr(>it) (Intercept) 6.5818 1.1883 8.936 5.539 0.000377 \*\*\*
NAP -2.8293 0.6849 7.9217 -4.131 0.003366 \*\*\*

This intercept and slope.

RANDOM INTERCEPT AND SLOPE MODEL: intercepts and slopes are allowed to vary IS THIS A GOOD MODEL for these data?

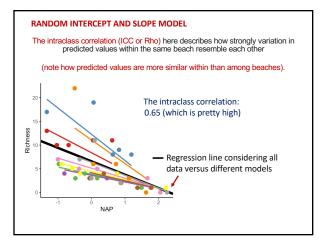
Random effects:
Groups Name Variance Std.Dev. Corr factor\_Beach (Intercept) 10.949 = 3.399
NAP 2.502 = 1.582 = 1.00
Residual 7.174 = 2.678
Number of obs: 45, groups: factor\_Beach, 9
Fixed effects:
Estimate Std. Error df t value Pr(-|t|)
(Intercept) 6.5818 1.1883 8.8936 5.539 0.000377 \*\*\*
NAP -2.8293 0.6849 7.9217 -4.131 0.003366 \*\*

The intraclass correlation (ICC or Rho) here describes how strongly variation in predicted values within the same beach resemble each other.

ICC = (10.949+2.502) / (10.949+2.502+7.174) = 0.65

(even higher than the previous random intercept model)

16



17

Which model to retain? The RANDOM INTERCEPT OR the RANDOM INTERCEPT AND SLOPE MODEL?

| Mathematical Companies of the Random Intercept OR the RANDOM INTERCEPT AND SLOPE MODEL?

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### Next – "Go big or go home": Going complex!



19

How do "competing" models compare with one another? Which model best fit the data?



Figure source: https://wires.onlinelibrary.wiley.com/doi/full/10.1002/wics.1607

20

Let's now consider different models, make them compete and select the one that best describe the same set of data (i.e., predict Richness).

$$R_{ij} = b_0 + b_1 \times NAP_{ij} + e_{ij}$$

MODEL 1: No interaction or main effect of exposure, i.e., just NAP under a random intercept model (as seen earlier):

I	$R_{ij} = b_0 + b_2 \times Exposure_j + e_{ij}$
MODEL 2:	No interaction or main effect of NAP i.e. just EXPOSURE
	No interaction or main effect of NAP, i.e., just EXPOSURE ndom intercept model:
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Competing models R_{ij} = b_0 + e_{ij} MODEL 5: Model with a fixed intercept and only random effects (i.e., the "simplest" model) \bullet \bullet \bullet \bullet mixed_model_IntOnly_NoFix <- lmer(Richness \sim 1 + (1) factor_Beach), REML = FALSE, data = RIKZ.data) \bullet \bullet \bullet \bullet Random effects: Groups Name Variance Std.Dev. factor_Beach (Intercept) 8.97 2.995 Residual 15.51 3.938 Number of obs: 45, groups: factor_Beach, 9 \bullet \bullet \bullet \bullet Fixed effects: Estimate Std. Error df t value Pr(>|t|) (Intercept) 5.689 1.158 9.000 4.912 0.000834 ***
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## 

26

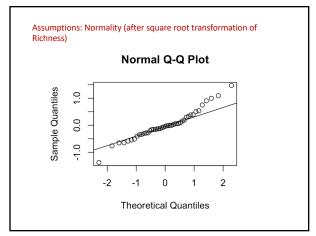
#### NOTES:

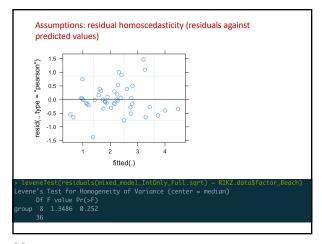
- We only considered the intercept only model. We could have considered for each model the intercept and slope model (Tutorial).
- We could have also considered all the fixed effect only: Intercept only NAP only Exposure only

NAP + Exposure NAP x Exposure (main effects + interaction).

3) And once all models are built, compare them using AIC.

The best model (amongst the ones we compared in this lecture; but more models in the tutorial)!  $R_{ij} = b_0 + b_1 \times NAP_{ij} + b_2 \times Exposure_j \\ b_3 \times (NAP_{ij} \times Exposure_j) + e_{ij}$  Random effects: Groups Name Variance Std.Dev. factor\_Beach (Intercept) 2.208 1.486 Residual 8.210 2.865 Number of obs: 45, groups: factor\_Beach, 9 Fixed effects: Estimate Std. Error df t value Pr(>|t|) (Intercept) 14.1320 2.0618 9.7520 6.854 5.02e-05 \*\*\* Exposure -5.5175 1.3936 49.7436 -3.959 0.000295 \*\*\* Exposure -5.2625 1.3583 9.9914 -3.874 0.003092 \*\* NAP:Exposure 2.0252 0.9155 40.2485 2.212 0.032688 \*





Assumptions: Recently shown that mixed-effects models are	
robust against normality and heteroscedastic assumptions	
Methods in Ecology and Evolution Society	
RESEARCH ARTICLE │ 🗇 Open Access │ 🍪 🕦	
Robustness of linear mixed-effects models to violations of distributional assumptions	
Holger Schielzeth 🗷 , Niels J. Dingemanse, Shinichi Nakagawa, David F. Westneat, Hassen Allegue, Céline Teplitsky, Denis Réale, Ned A. Dochtermann, László Zsolt Garamszegi, Yimen G. Araya-Ajoy See fewer authors 🔨	
First published: 12 June 2020   https://doi.org/10.1111/2041-210X.13434   Citations: 13	