

CHEM 206 section 01

LECTURE #24

Fri. April 04, 2008

## LECTURE TOPICS:

**TODAY'S CLASS:** start Ch.18

**NEXT CLASS:** continue Ch.18

(1)

## Chapter 18: OTHER ASPECTS OF AQUEOUS EQUILIBRIA

- Application of eqm concepts to control of pH (buffers), analysis of solutions (titrations), & understanding of solubility

### Outline (but not in this order here)

- 18.3 Acid-base titrations
- 18.1 The Common ion effect
- 18.2 Controlling pH: buffer solutions
- 18.4 Solubility of salts
- 18.5 Precipitation reactions

(Not responsible for 18.6 & 18.7)

### Chapter Goals

- Understand the common ion effect
- Understand the control of pH in aqueous solutions with buffers
- Evaluate the pH in the course of acid-base titrations
- Apply chemical equilibrium concepts to the solubility of ionic compounds

(2)

## 18.3 Titrations & titration curves

TITRATION = volumetric analysis

- Exploits known chemical rxn

e.g., acids & bases:  $\text{H}_3\text{O}^+ + \text{OH}^- \rightarrow 2 \text{H}_2\text{O}$

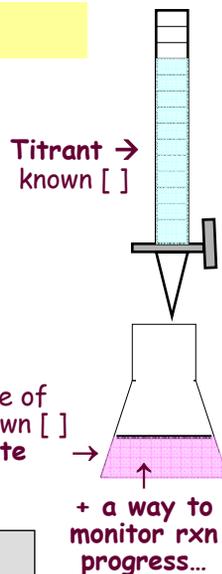
NOTE: This reaction goes to completion  
i.e.,  $K$  is large ( $= 1/K_w = 10^{14}$ )  
so we often forget that it's an eqm...

- Typical titration reactions:



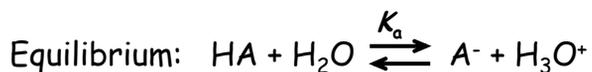
**PROCEDURE:** Titrant + Analyte  $\rightarrow$  Rxn...  
Measure volume of titrant required to reach  
perfect stoichiometric completion of rxn  
= "equivalence point"

(3)



### Titration & eqm knowledge: e.g., weak HA with NaOH...

1.) Initially: have a solution of weak acid in water...



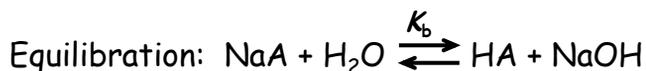
*If  $[\text{HA}]_0$  is known,  
could calculate  
solution's initial pH...*

2.) Then, start disturbing this eqm:



*Draws HA dissociation  
fwd by consuming  $\text{H}_3\text{O}^+$   
 $\Rightarrow$  net effect same as  
if deprotonates HA.*

3.) At equiv. point: enough titrant added to consume all HA  
now have a solution of the acid's salt...  
...whose rxn with water comes to eqm:



*Could calculate  
solution's pH...*

(4)

FOR QUANTITATIVE PURPOSES, IT IS VERY IMPORTANT  
THAT WE KNOW EXACTLY WHEN EQUIV. PT. IS REACHED.

## Titration calculations

(assuming we can accurately determine the equivalence point)

### Dealing with a Strong Acid - Strong Base Titration

Simple: **A stoichiometry problem** (review from Chem 205; see Ch.5)

- assume rxn goes to completion
- remaining solution is neutral (pH = 7)
- no need to think much about eqm, since reaction is so very product favoured!

### Dealing with a Weak - Strong Titration (either way)

Step 1: **A stoichiometry problem**

- assume titration rxn goes to completion
- then determine species (salt!) remaining in solution at equivalence point
- will include a weak acid's (or base's) conjugate!

Step 2: **An equilibrium problem: salt equilibrates with water**

- salt will equilibrate with water (A/B chemistry)
  - calculate pH of this weak A/B solution!
- (5)

### Ex.: How much lactic acid is in our sample?

You titrate a 25.0 mL sample of lactic acid ( $\text{HC}_3\text{H}_5\text{O}_3$ ,  $K_a=1.4\times 10^{-4}$ ) with  $8.00\times 10^{-2}$  M NaOH. It requires 31.35 mL of titrant.

- (a) What mass of lactic acid was in the sample?  
(b) What is the pH of the sample at the equivalence point?

(a) **STEP 1: Deal with stoichiometric rxn of acid & base:**



$$V = 0.0250 \text{ L}$$

$$C = ?$$

$$n = ?$$

$$V = 0.03135 \text{ L}$$

$$C = 8.00\times 10^{-2} \text{ M}$$

$$n = (0.03135 \text{ L})\times(8.00\times 10^{-2} \text{ mol/L})$$

$$= 2.5080\times 10^{-3} \text{ mol} \quad \text{note: kept extra SFs...}$$

At the equivalence point: perfect stoichiometric ratio (1:1)

$$\begin{aligned} \# \text{ moles acid initially present} &= \# \text{ moles base added} \\ &= 2.508\times 10^{-3} \text{ mol} \end{aligned}$$

In original sample:

$$\text{Mass HC}_3\text{H}_5\text{O}_3 = \text{MM} \times n$$

$$= (90.079 \text{ g/mol}) \times (2.508\times 10^{-3} \text{ mol})$$

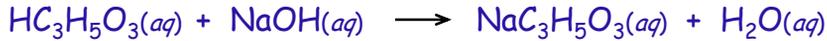
$$= 0.226 \text{ g was present in the 25.0 mL sample}$$

*note: 3 SF in data...*

(6)

STEP 2: EQUILIBRIUM...

(b) Calculate the pH of the solution at the equiv. point...



After this product-favoured acid-base rxn:  
what is the dominant species present in the solution?

**Lactate equilibrates with water: how much is initially present?**

- All lactic acid converted to lactate:  $\#n_{\text{lactate}} = 2.508 \times 10^{-3} \text{ mol}$
- Total volume of solution at equiv.pt:  $V = V_{\text{sample}} + V_{\text{titrant}}$   
 $= 0.0250 \text{ L} + 0.03135 \text{ L}$   
 $= 0.05635 \text{ L}$
- Thus: concentration of lactate initially:  $C = 0.04451 \text{ M}$

**Lactate equilibrates with water: how basic is lactate?**

- $K_a$  for lactic acid =  $1.4 \times 10^{-4}$
  - $K_b$  for lactate (conjugate base) =  $K_w / K_a$   
 $= 1 \times 10^{-14} / 1.4 \times 10^{-4}$   
 $= 7.143 \times 10^{-11}$  1 extra SF...
- (7)

(b) Calculate the pH of the solution at the equiv. point...

**Lactate equilibrates with water:**



Initial	0.04451 M	solvent...	0	0
Change	- x	---	+ x	+ x
Eqm	0.04551 - x	---	+ x	+ x

$$K_b = \frac{[\text{C}_3\text{H}_5\text{O}_3^-][\text{OH}^-]}{[\text{HC}_3\text{H}_5\text{O}_3]} \Rightarrow 7.143 \times 10^{-11} = \frac{x^2}{0.04451 - x}$$

Note that  $K \ll 1000x$  smaller than initial [ ]  
...therefore CAN use approximation

pH = 14 - pOH  
 $= 14 - [-\log(1.78 \times 10^{-6})]$   
 $= 8.251$  mildly basic

$$7.143 \times 10^{-11} \approx \frac{x^2}{0.04451}$$

$$x = \sqrt{(0.04451 \times 7.143 \times 10^{-11})}$$

$$x = 1.78 \times 10^{-6} \text{ M} = [\text{OH}^-]$$

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## How to monitor an acid-base titration? (to accurately determine equivalence point)



- 1.) using a chemical "indicator"
  - = a substance whose colour depends on pH
  - cheap, easy...but must be careful (& know pH at eq.pt....)
  - CHEMISTRY BEHIND THIS → end of 18.3
- 2.) using a pH meter
  - electrode:  $H^+$  passes through thin glass membrane
  - a redox rxn of  $H^+$  creates current proportional to  $[H_3O^+]$
  - costs a little more... & a bit more time-consuming...
  - but: can be automated!
  - AND reveals information about species

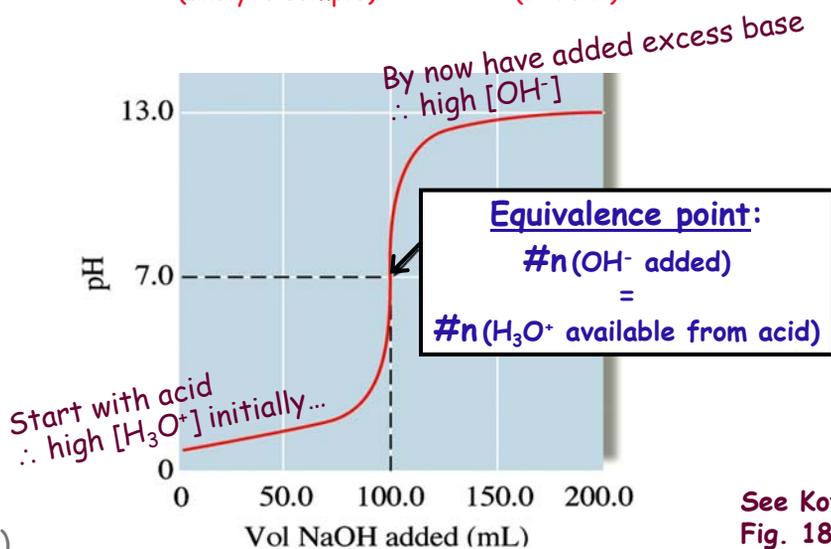


**Titration curve (or pH curve)**  
= plot of pH of solution being analyzed  
versus amount of titrant added

(9)

### A1) TITRATION of "STRONG" with "STRONG"

Z.'s Figure 15.1: Titration curve for the titration of  
50.0 mL of 0.200 M  $HNO_3$  with 0.100 M NaOH  
(analyte sample) (titrant)



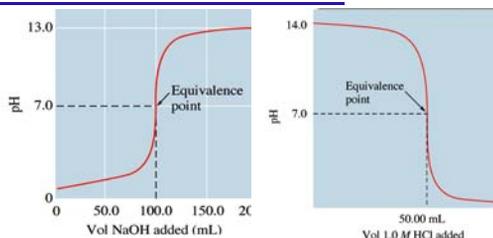
(10)

**GENERAL SHAPES OF TITRATION CURVES:**  
 indicative of strengths of acids/bases involved  
 → helpful when your sample is an unknown acid/base

See Kotz  
 Fig.18.x  
 x=4,5,7

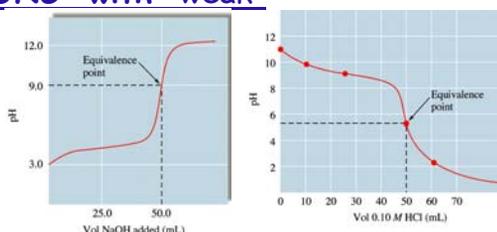
### A) TITRATION of "STRONG" with "STRONG"

- pH curves are sharp & symmetric
- at equiv. pt.: pH = 7 because have soln of "very weak" conjugate acid (or base)



### B) TITRATION of "STRONG" with "weak"

- pH curves not symmetric...
- at equiv. pt.: = soln of conjugate weak acid *or* weak base  
 ⇒ pH ≠ 7



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### Why is the titration curve's shape different when a weak acid or base is involved?

Because of the ACID-BASE PROPERTIES of the "SALT" formed during titration's rxn: acid + base → salt + water

strong acid  
 strong base

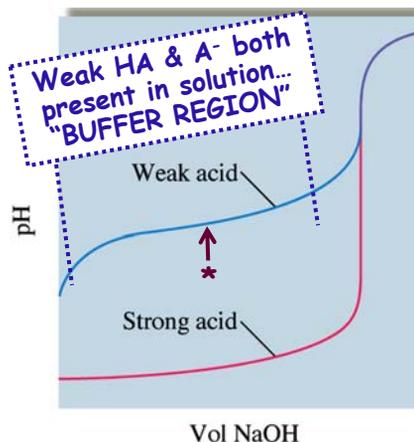
Smooth pH ↑ due to consumption of H<sub>3</sub>O<sup>+</sup>.  
 Salt too weak to influence pH.

weak acid  
 strong base

Anion is a weak base.  
 ⇒ pH ↑ quickly at 1<sup>st</sup> due to action of A<sup>-</sup>.  
 ⇒ later: buffered

strong acid  
 weak base

Cation is a weak acid...  
 (see Fig.18.7)



Halfway to equivalence point (\*), ½ of analyte is "neutralized"

- at that moment: [HA] = [A<sup>-</sup>] ⇒ therefore pH = acid's pK<sub>a</sub>
- implication: can use titrations to help identify unknown species too!

## Acid-Base Indicators = colourful weak acids/bases

An INDICATOR is: a weak acid "H-In" OR a weak base "In<sup>-</sup>"  
whose conj. base/acid is a different colour



**STRATEGY:** once analyte completely consumed by titrant (**equiv. point**),  
next drop of titrant causes indicator to change colour (**end point**)

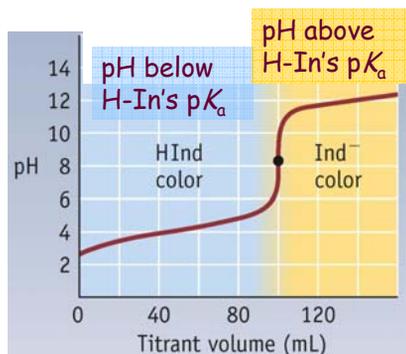
**Indicator error** = difference between volume of titrant used (end pt.)  
vs. should have used (equiv.pt.)

**TO MINIMIZE INDICATOR ERROR,  
CHOOSE INDICATOR WITH...**

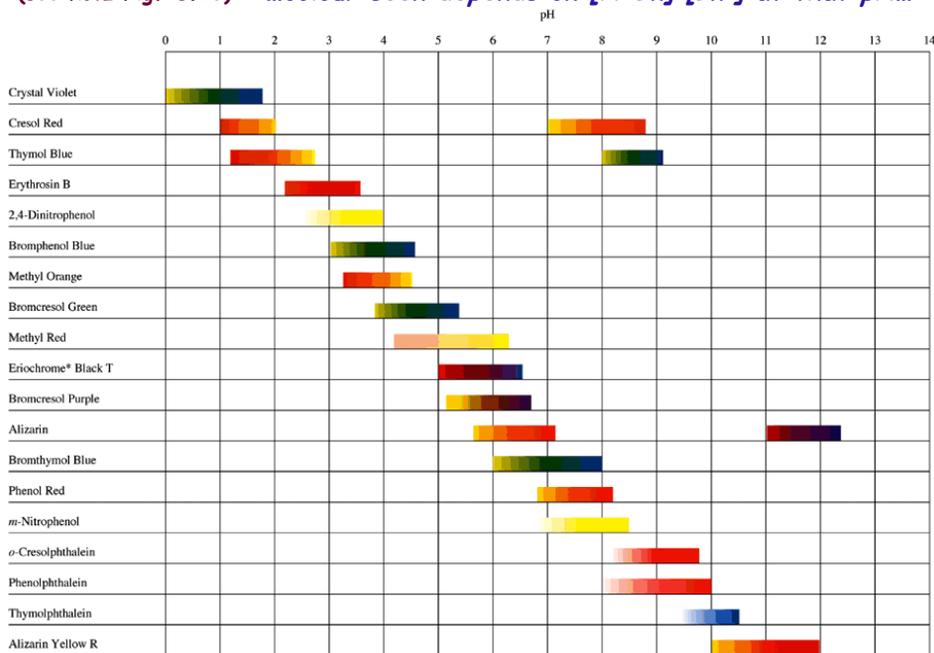
- H-In with  $pK_a = \text{pH}$  of equiv. pt.
- **THUS:** Colour change occurs as close as possible to pH of equivalence point

see Fig.18.9 →

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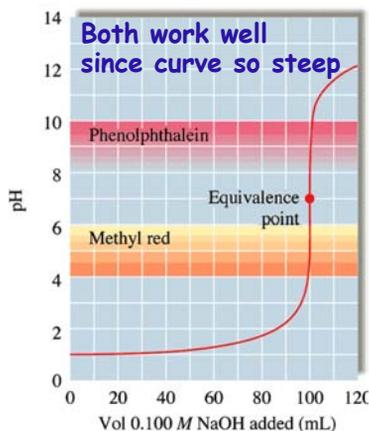


**Z.'s Figure 15.8:** pHs of colour change for common A/B indicators  
(see Kotz Fig.18.10) ...colour seen depends on  $[\text{H-In}]:[\text{In}^-]$  at that pH...

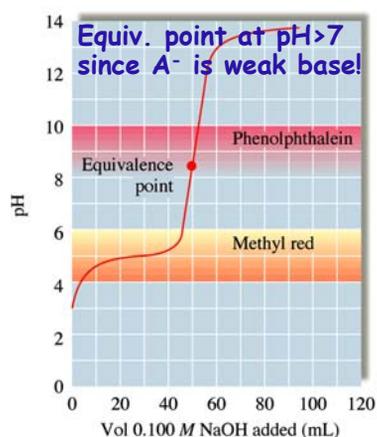


**Choosing the right indicator requires forethought...**  
**...in order to minimize indicator error (=  $V_{\text{end pt.}}$  vs.  $V_{\text{equiv. pt.}}$ )**

Z.'s Fig. 15.9: Titration of strong acid with strong base  
 100.0 mL of 0.10 M HCl  
 with 0.10 M NaOH.



Z.'s Fig. 15.10: Titration of weak acid with strong base  
 50 mL of 0.1 M  $\text{HC}_2\text{H}_3\text{O}_2$   
 with 0.1 M NaOH.



### Homework: which indicator would be most appropriate?

Suggestion: solve this on your own & compare with your classmates

Imagine you are required to do repeated analyses of samples containing sodium benzoate ( $\text{NaC}_6\text{H}_5\text{COO}$ ), which is used as a preservative. You are planning to manually perform titrations with HCl using a pH indicator (not a pH meter). Based on the expected pH at the equivalence point, which indicators (from Z.Fig.15.8 list) would be suitable choices? If more than one indicator would be suitable, please explain which one would be easiest to use, and why.

Relevant details:

- Your samples will be 20.0 mL, with  $[\text{NaC}_6\text{H}_5\text{COO}] \approx 0.04 \text{ M}$ .
- You are planning to use a titrant solution of  $[\text{HCl}] = 0.03755 \text{ M}$ .

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## ASSIGNED READINGS:

### BEFORE NEXT CLASS:

**Read:** section 18.3

**Practice:** A/B & titration calculations & concepts  
using  $pK_a$  to identify speciation at different pHs

+ WORK ON Problems from Ch.17 & 18.3

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